

Solving Inequalities

2x + 4 ≤ 10

x	2x + 4 ≤ 10	
1	6 ≤ 10	✓
2	8 ≤ 10	✓
3	10 ≤ 10	✓
4	12 ≤ 10	×
5	14 ≤ 10	×

Equation: 2x + 4 = 10, solution: x = 3



Inequality: 2x + 4 ≤ 10, solution: x ≤ 3



Rules for inequalities

- $A \leq B \Leftrightarrow A + C \leq B + C$
- $A \leq B \Leftrightarrow A - C \leq B - C$
- If $C > 0$, then $A \leq B \Leftrightarrow CA \leq CB$
- If $C < 0$, then $A \leq B \Leftrightarrow CA \geq CB$
- If $A > 0$ and $B > 0$, then $A \leq B \Leftrightarrow \frac{1}{A} \geq \frac{1}{B}$
- If $A \leq B$ and $C \leq D$, then $A + C \leq B + D$

Example 1: Solve inequality and sketch the solution set.

3x - 1 ≥ 3 + x



Example 2: Solve the inequality.

$$5 \leq 3x - 4 \leq 14$$

Solving Nonlinear Inequalities

The sign of a product or quotient

- Even number of negative terms = positive.
- Odd number of negative terms = negative.

Guidelines for Solving Nonlinear Inequalities

1. Move All Terms to One Side.
2. Find the Intervals. ()()
3. Make a Table or Diagram.
4. Solve.

Example 3: Solve the nonlinear inequality

$$x^2 \leq x + 2$$



Example 4: Solve the nonlinear inequality

$$(x - 2)^2(x - 3)(x + 1) \leq 0$$

Example 5: Solve the nonlinear inequality

$$\frac{3 + x}{3 - x} \geq 1$$

